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|---|--|------------------------------------|--|
| 1. <b>2-1 Inductive Reasoning</b>               | Reasoning based on observation of patterns or past experiences.  | 19. <b>2-4 Law of Syllogism</b>    | If "p then q" is true, and "q then r" is true, then "p then r" is true. Similar to the Transitive Property. Example: If Jane is sick, she will be absent. If she is absent, she will miss her classwork. Jane is sick on Tuesday. Therefore... |
| 2. <b>2-1 Conjecture</b>                        | An educated guess based on inductive reasoning. Expected to be true, but not yet proved. Can be true or false.   | 20. <b>2-5 Reflexive Property</b>  | $a = a$ , or $xyz = xyz$   |
| 3. <b>2-1 Counterexample</b>                    | A single, false example that disproves a conjecture.   | 21. <b>2-5 Symmetric Property</b>  | If $a = b$ then $b = a$ , or if $3 = x$ , then $x = 3$   |
| 4. <b>2-2 Conditional</b>                       | An if-then statement. Usually "if p then q" or " $p \rightarrow q$ ".  | 22. <b>2-5 Transitive Property</b> | If $a = b$ and $b = c$ , then $a = c$ . Similar to the Law of Syllogism.   |
| 5. <b>2-2 Hypothesis</b>                        | The part p following if. "hyPotesis"   | 23. <b>2-5 Proof</b>               | A convincing argument that uses deductive reasoning.   |
| 6. <b>2-2 Conclusion</b>                        | The part q following then. "QonClusion"  | 24. <b>2-6 Postulate or Axiom</b>  | An accepted statement of fact; does not require further proof.   |
| 7. <b>2-2 Truth Value</b>                       | Whether a conditional is true (T) or false (F).  | 25. <b>2-6 Theorem</b>             | A conjecture which must first be proved true using postulates and/or already proved theorems.  |
| 8. <b>2-2 Converse</b>                          | Exchange (switch / swap / reverse) the hypothesis and conclusion. Usually "if q then p" or " $q \rightarrow p$ ".  | 26. <b>2-2 Compound Statement</b>  | 2 or more statements that are joined (as a conjunction or disjunction).  |
| 9. <b>2-2 Inverse</b>                           | Negate (opposite) both the hypothesis and conclusion. Usually "if not p then not q" or " $\sim p \rightarrow \sim q$ ".  | 27. <b>2-2 Conjunction</b>         | Joining of 2 or more statements with the word AND; written as " $s \wedge j$ "; only true if both are true.  |
| 10. <b>2-2 Negation</b>                         | The opposite of the original conditional. The negation of p is $\sim p$ . The negation of $\sim p$ is p. The negation of "is orange" is "is not orange." The negation of "is not cold" is "is cold." | 28. <b>2-2 Disjunction</b>         | Joining 2 or more statements with the word OR; written as " $s \vee j$ "; true if either statement is true.  |
| 11. <b>2-2 Contrapositive</b>                   | Switch (reverse) AND Negate both the hypothesis and conclusion. Usually "if not q then not p" or " $\sim q \rightarrow \sim p$ ".  |                                    |  |
| 12. <b>2-2 Conditional &amp; Contrapositive</b> | These share the same truth value. (If one is true, the other must also be true. If one is false, the other must also be false.)  |                                    |  |
| 13. <b>2-2 Converse &amp; Inverse</b>           | These share the same truth value. (If one is true, the other must also be true. If one is false, the other must also be false.)  |                                    |  |
| 14. <b>2-3 Biconditional</b>                    | Bi -- Both Directions. A single true statement that combines a true conditional and its true converse. Usually "p if and only if q" or "p iff q" or " $p \leftrightarrow q$ ".                       |                                    |  |
| 15. <b>2-3 Definition</b>                       | True and reversible. Example: A penny is a coin worth one cent, and a coin worth one cent is a penny. No counterexample exists.  |                                    |  |
| 16. <b>2-5 ∴</b>                                | Therefore  |                                    |  |
| 17. <b>2-4 Deductive Reasoning</b>              | Reasoning logically from given statements, facts, rules, or properties to a conclusion.  |                                    |  |
| 18. <b>2-4 Law of Detachment</b>                | If "p then q" is a true conditional statement, and p is true, then q is true. Example: If it rains, then Joe will carry an umbrella. It is raining today. Therefore, ...                             |                                    |  |